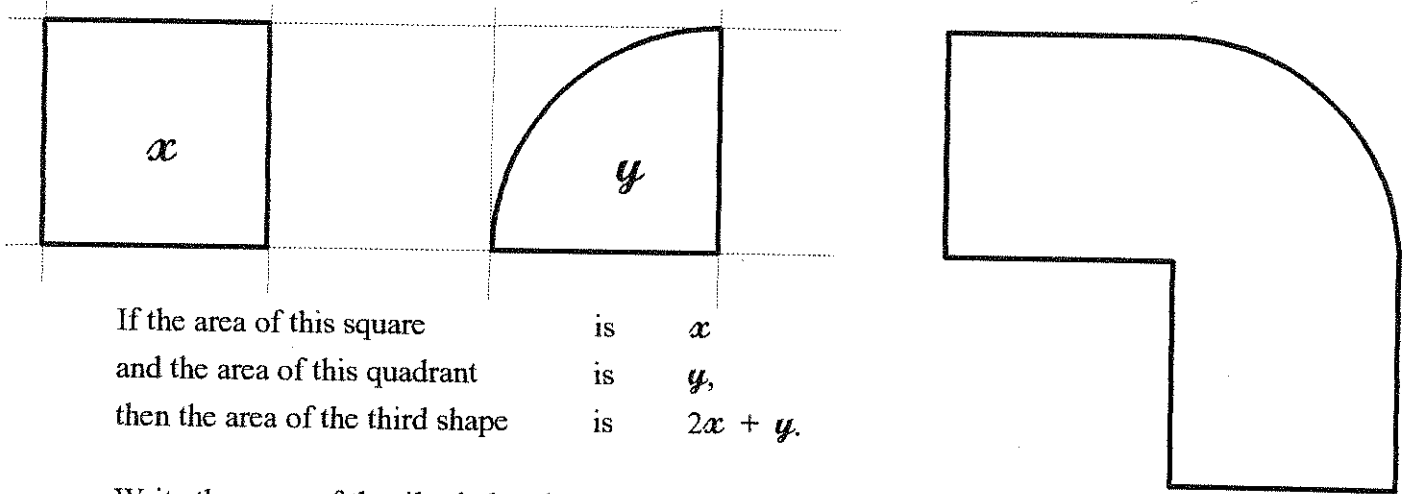


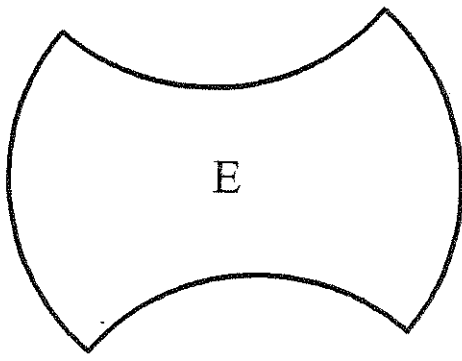
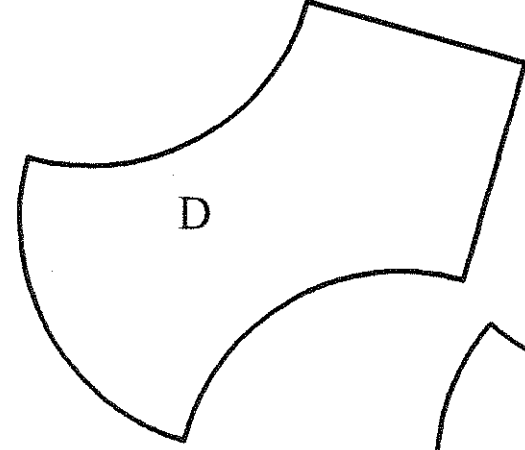
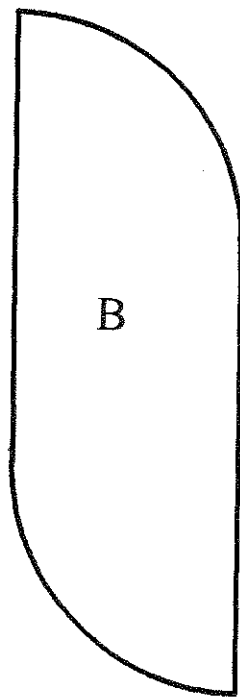
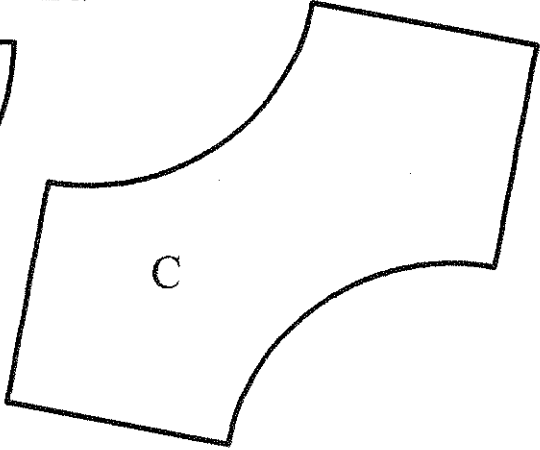
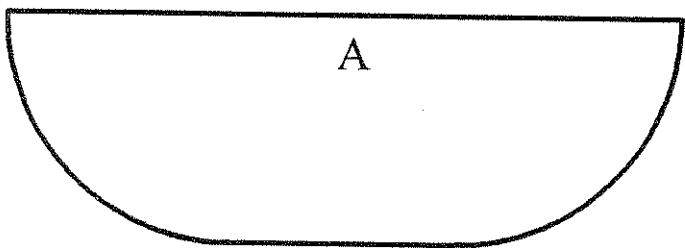
Sheet C1

The Easy TakTiles



If the area of this square is x
 and the area of this quadrant is y ,
 then the area of the third shape is $2x + y$.

Write the areas of the tiles below in terms of x and y .
 Draw in lines to show the squares and quadrants.



- $a =$
- $=$
- $b =$
- $=$
- $c =$
- $=$
- $d =$
- $=$
- $e =$
- $=$

NOTE: Keep this sheet for reference.

Sheet C2

Shapes Made of TakTiles

Show how Shape 1 can be made by fitting tiles A, C and D together.
Draw lines where they join.

Use the area of each tile (from Sheet C1) to find the total area of Shape 1.
Check your answer by adding up (and subtracting) squares and quadrants.

Shape 1

Area = $a + c + d$
 = $(x + 2y) + ($
 =

Shape 2

Area =
 =
 =

Shape 3

Area =
 =
 =

Now tackle Shapes 2 and 3 in the same way.

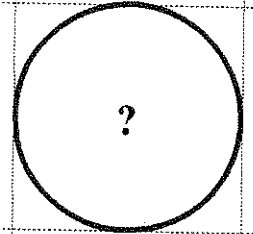
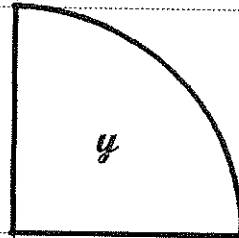
Explain to your neighbour how you arrived at each of your answers.

Sheet C3

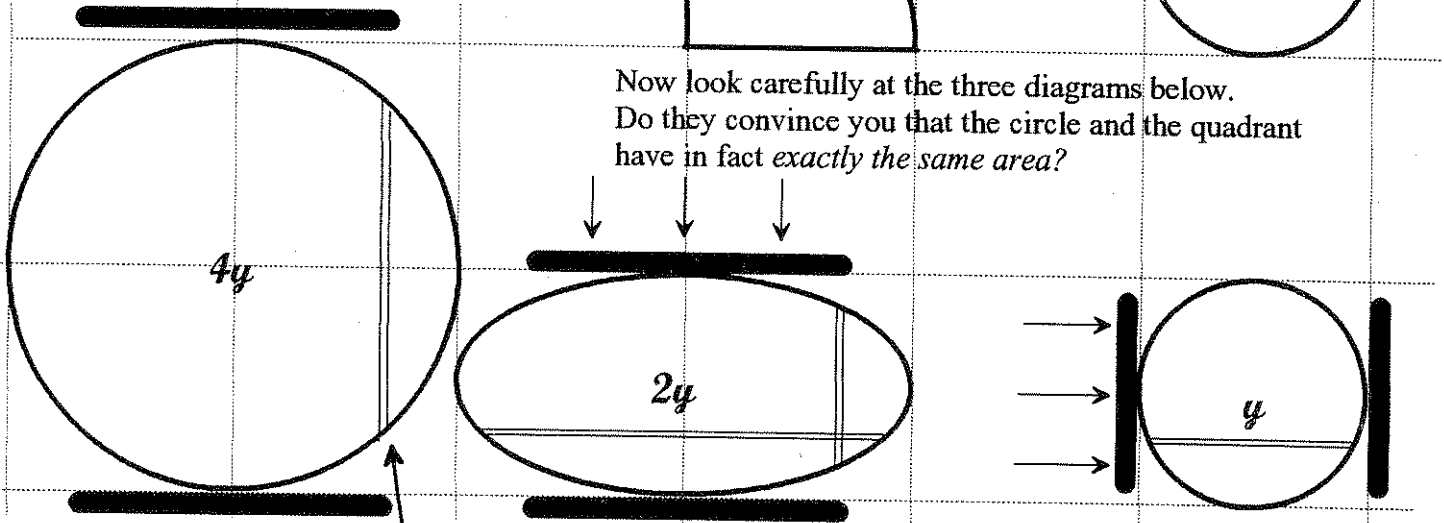
'Squashing' the Circle

Compare the area of the quadrant, y , with the area of the circle.

Which do you think is the bigger?



Now look carefully at the three diagrams below. Do they convince you that the circle and the quadrant have in fact *exactly the same area*?

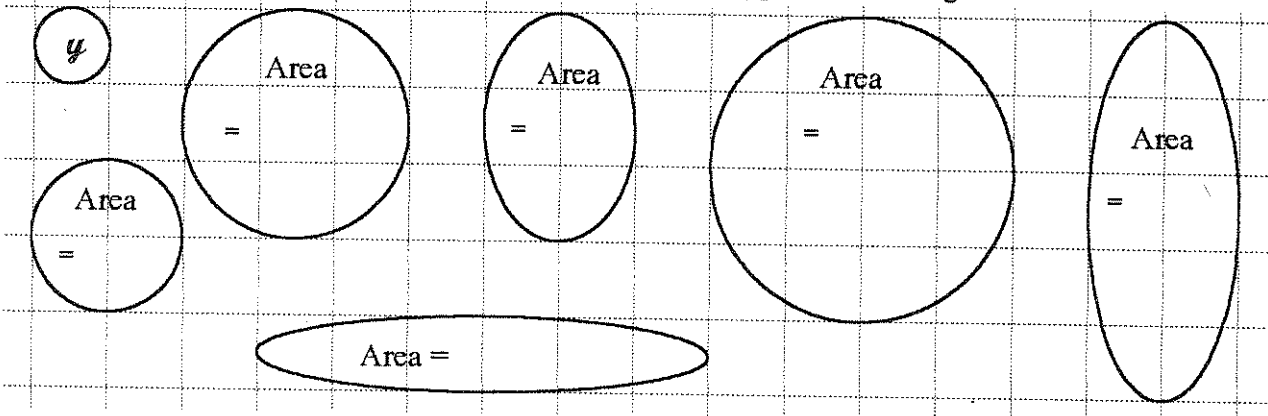


Think of it this way:

Step 1 The large circle above has area $4y$. If it is squashed to *half* its original height, then the length (and area) of this strip in it is *halved*. Think of the circle *all* cut up into strips like this, and you'll see that its total area must also be halved. So the area of the oval (or **ellipse**) is $2y$.

Step 2 Squash the ellipse horizontally until it is again a circle. Using the same reasoning we see that once again the area is halved. So the small circle has area y , the area of the quadrant.

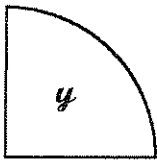
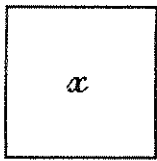
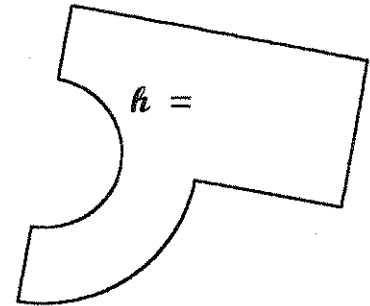
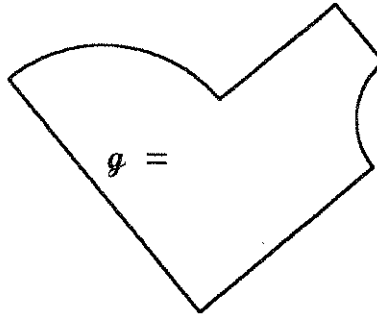
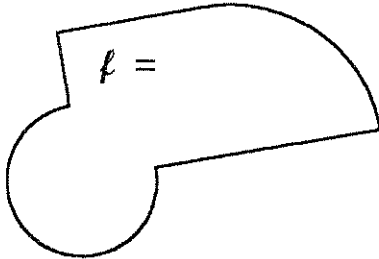
The *opposite* process to 'squashing' is '**stretching**'. By 'stretching' the small circle with area y , find the area of each of the other shapes. Use the same type of reasoning.



Sheet C4

The Other TakTiles

Find the areas of tiles F, G and H. It will help if you draw light pencil lines to divide them up into squares and quadrants.



Look at Shape 4. Find its area in terms of x and y :

(a) By adding squares and quadrants

Area =

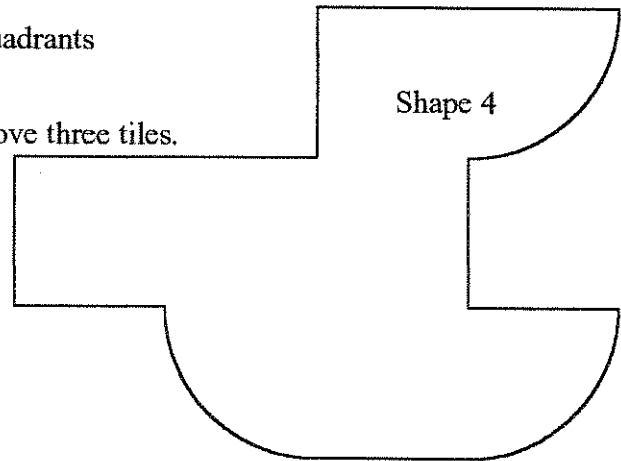
(b) By making it with the above three tiles.

(Show how by drawing lines.)

Area = $f + g + h$

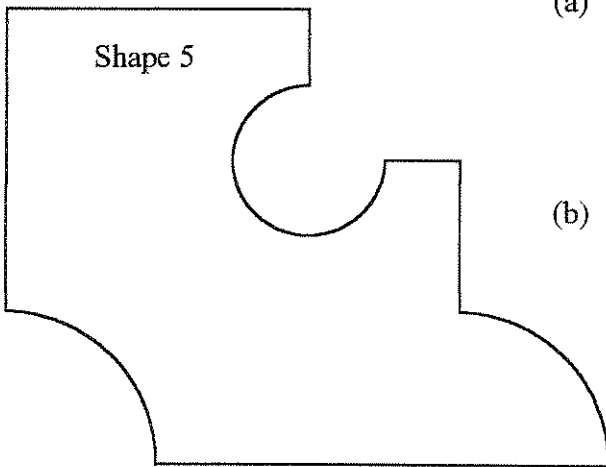
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These two areas should be the same. Are they?

Make Shape 5 using three tiles. Work out its area by the above two methods.



(a) Area of shape =

=

=

(b) Area of shape =

=

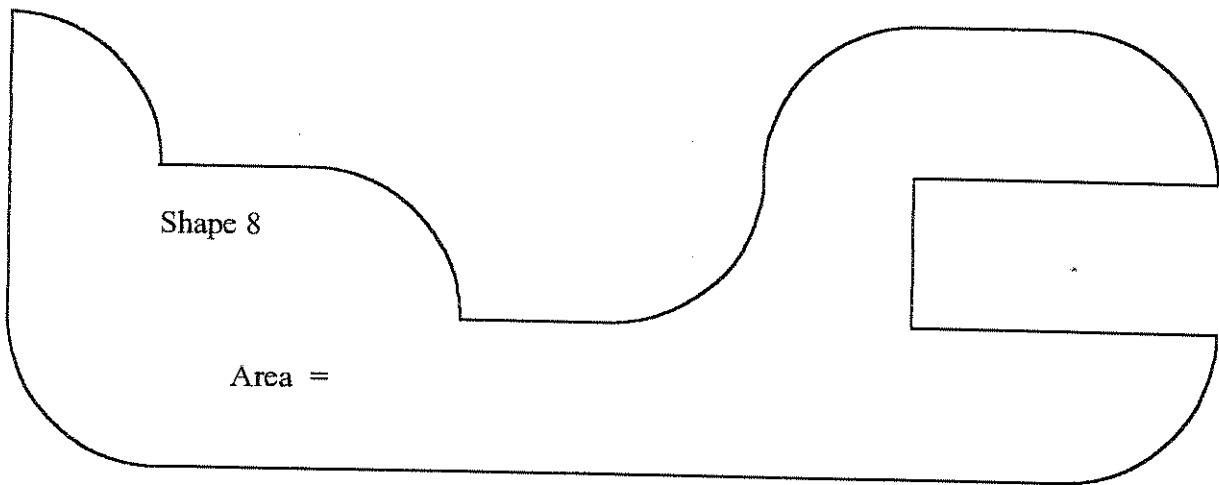
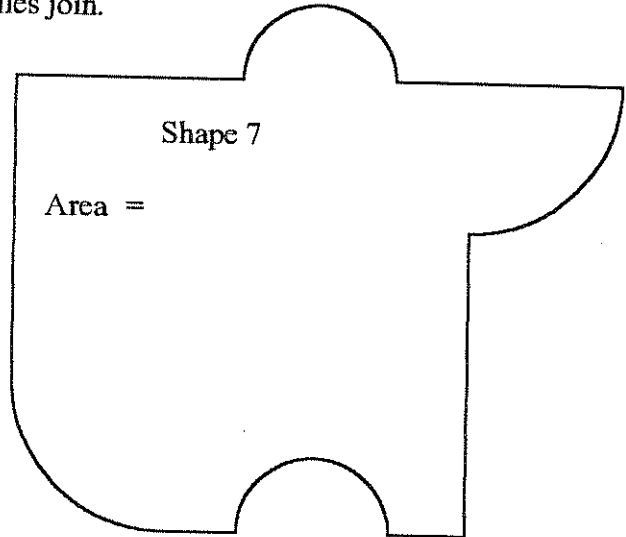
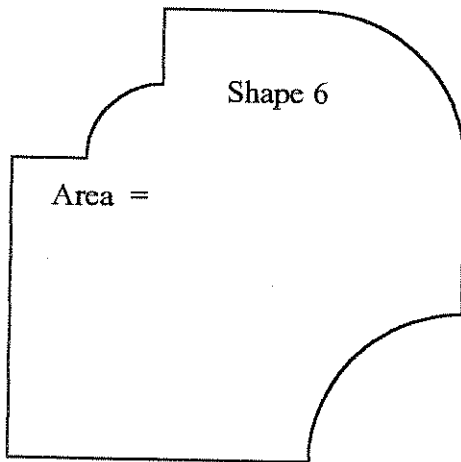
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Did you get the same answer?

Sheet C5

Four More Shapes

Make up these four shapes with TakTiles, first drawing light pencil lines to show the squares and quadrants. Draw heavy lines to show where the tiles join.



Find the area of each shape in terms of x and y .

Use the first method in the diagram above, and then use the second method below.

Area of: Shape 6 =

Shape 7 =

Shape 8 =

=

=

=

=

=

=

Were the answers you got using each method the same?

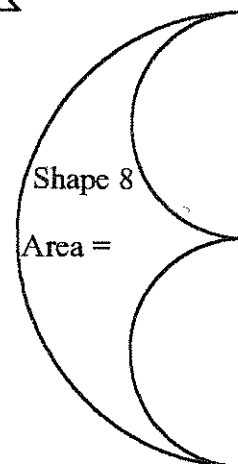
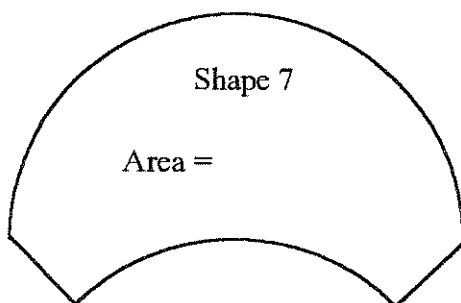
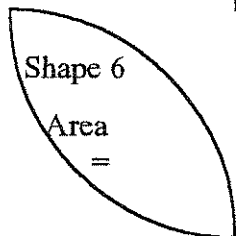
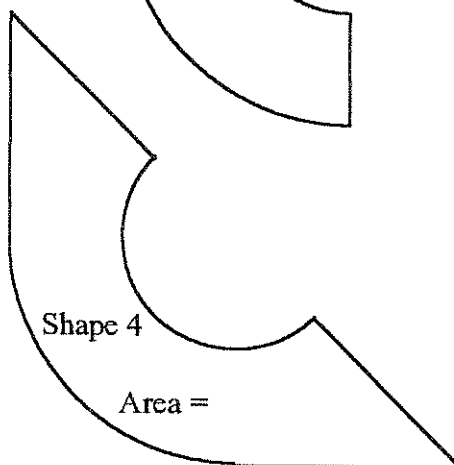
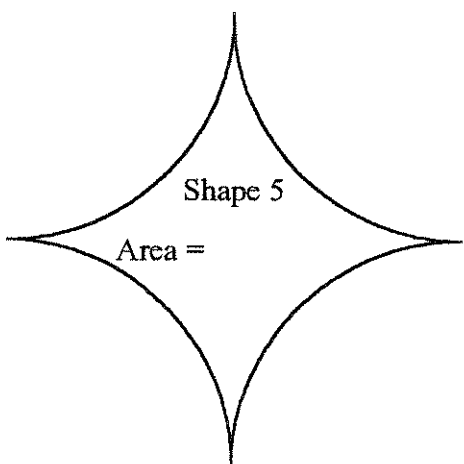
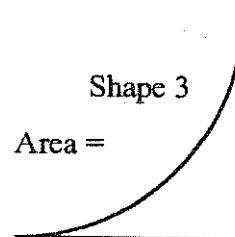
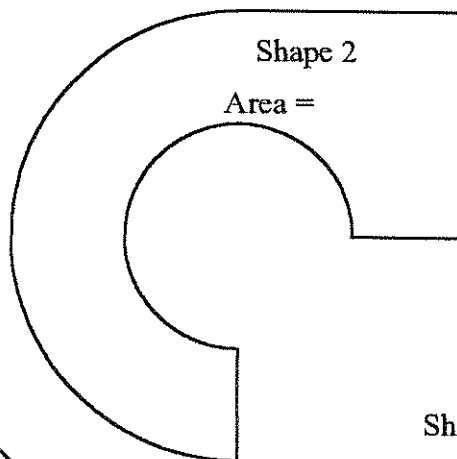
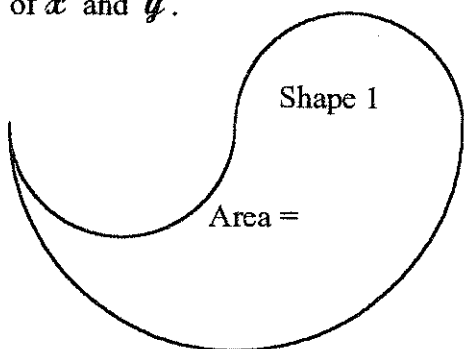
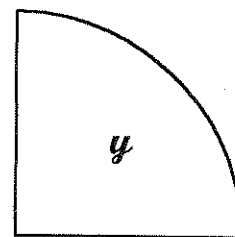
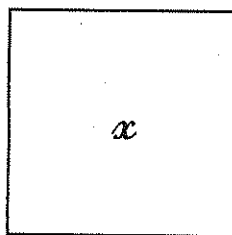
Sheet C6

Tricky Shapes

Here are some more difficult shapes that cannot be made using the tiles. Choose one that looks easy, and find its area in terms of x and y .

Now try the other ones.

All their areas can be expressed in terms of x and y .



ALGEBRA THROUGH GEOMETRY

NAME(S): CLASS:

Each square is the same size as the shape named x .
The sheet can help you work out the area of each shape.
You might trace the shapes and then remove them to work out the area.

